

Convection (part 4):

# Compressible mantle convection

# Concepts for today

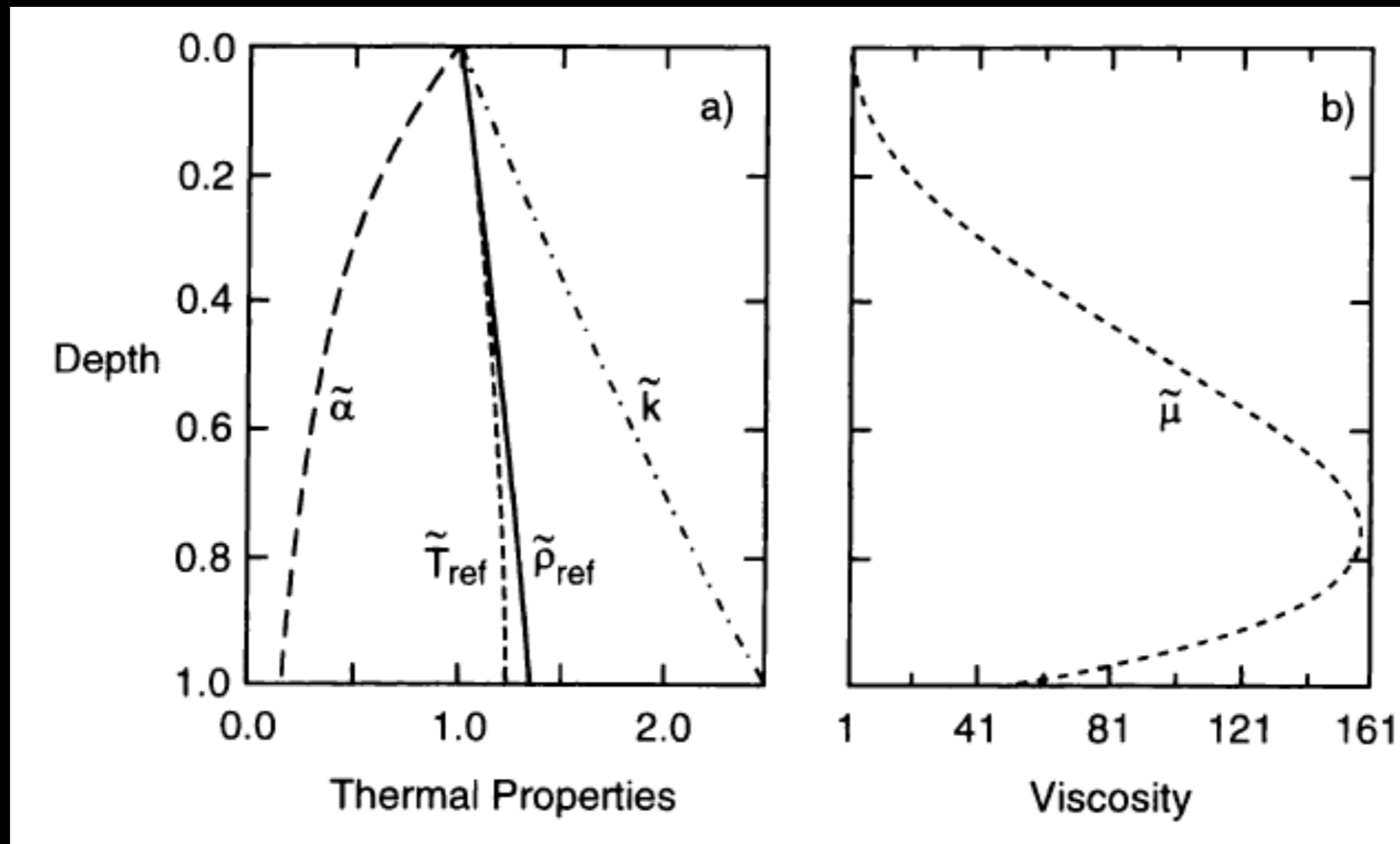
- **Compressible formulation for MC**
- **Effects of compressibility**
  - **on convective planform/structures**
  - **on energetics of the convection (additional heating / cooling terms)**
- **Feedback between temp-dep visc & compressibility**
- **Bullen's Parameter**

# Additional references

- *Mantle Convection in Earth + Planets*  
Schubert, Turcotte, and Olson (2001)
- King et al., *GJI*, 2010

# Depth-dependent material properties

- Material transport properties are depth-dependent
  - including: thermal expansivity, thermal conductivity, viscosity



Zhang and Yuen, PEPI, 1996

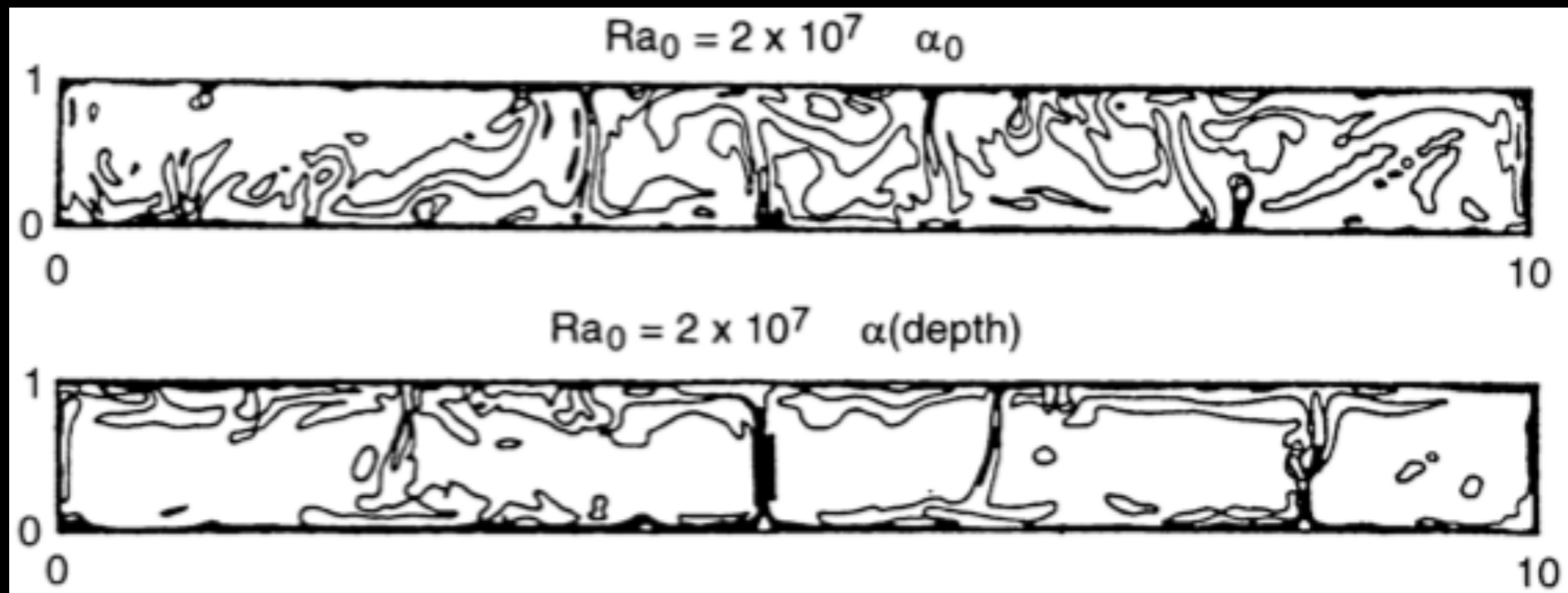
# Depth-dependent material properties

- Material transport properties are depth-dependent
  - including: thermal expansivity, thermal conductivity, viscosity
  - effective Ra decreases with depth

$$Ra = \frac{\rho_r^2 \alpha_r \Delta T_r c_p g_r L^3}{\eta_r k_r}$$

# Depth-dependent material properties

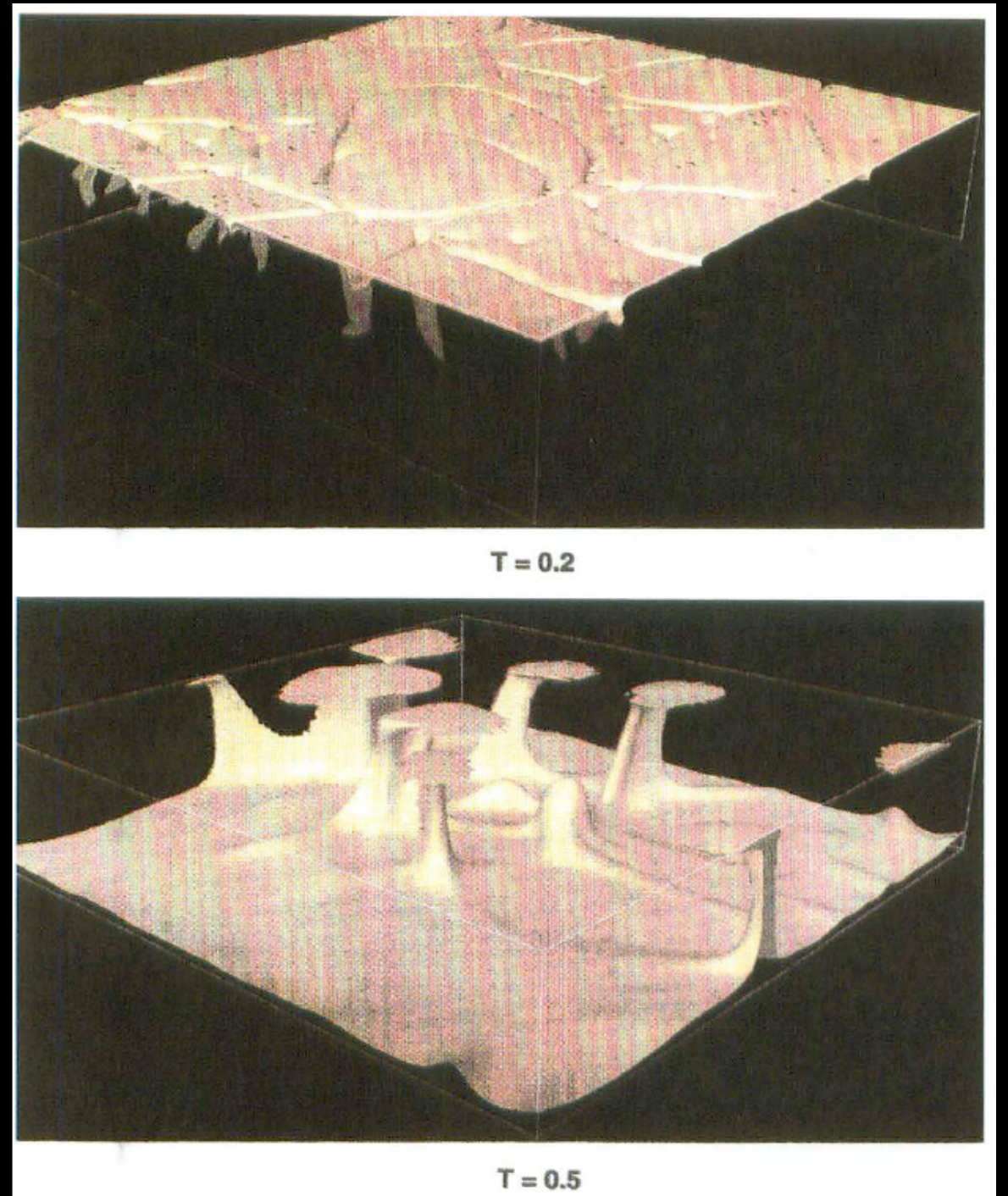
- Material transport properties are depth-dependent
  - including: thermal expansivity, thermal conductivity, viscosity
  - effective Ra decreases with depth
  - creates asymmetry between upwelling and downwelling structures



Hansen et al., *Phys Fluid*, 1993

# Effect on convective instabilities

- Convection in upper mantle has smaller-wavelength features and more chaotic
- Lower mantle structures are more organized and less time-dependent

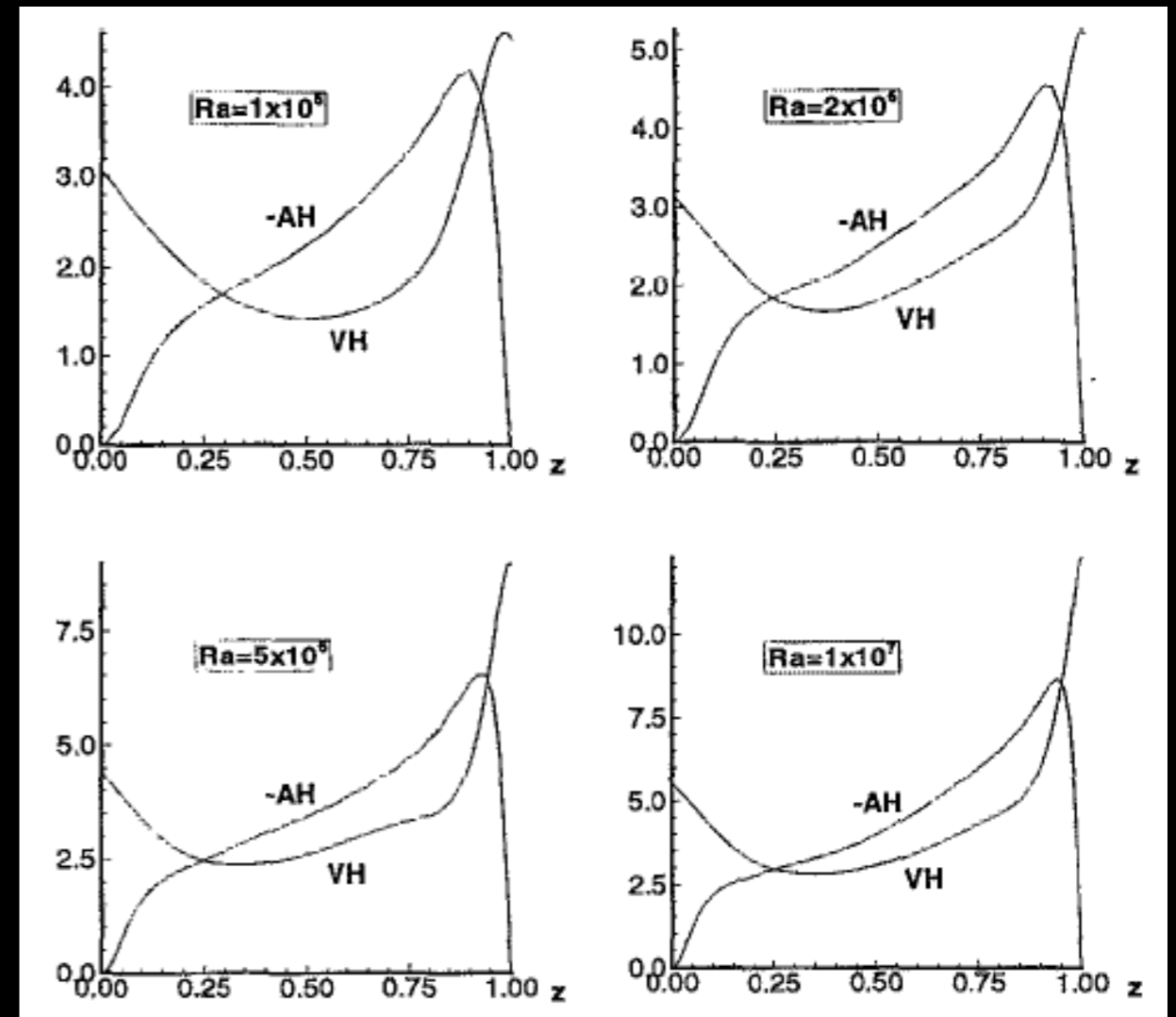


*Balachandar et al., Phys Fluid, 1993*



# Additional heating terms

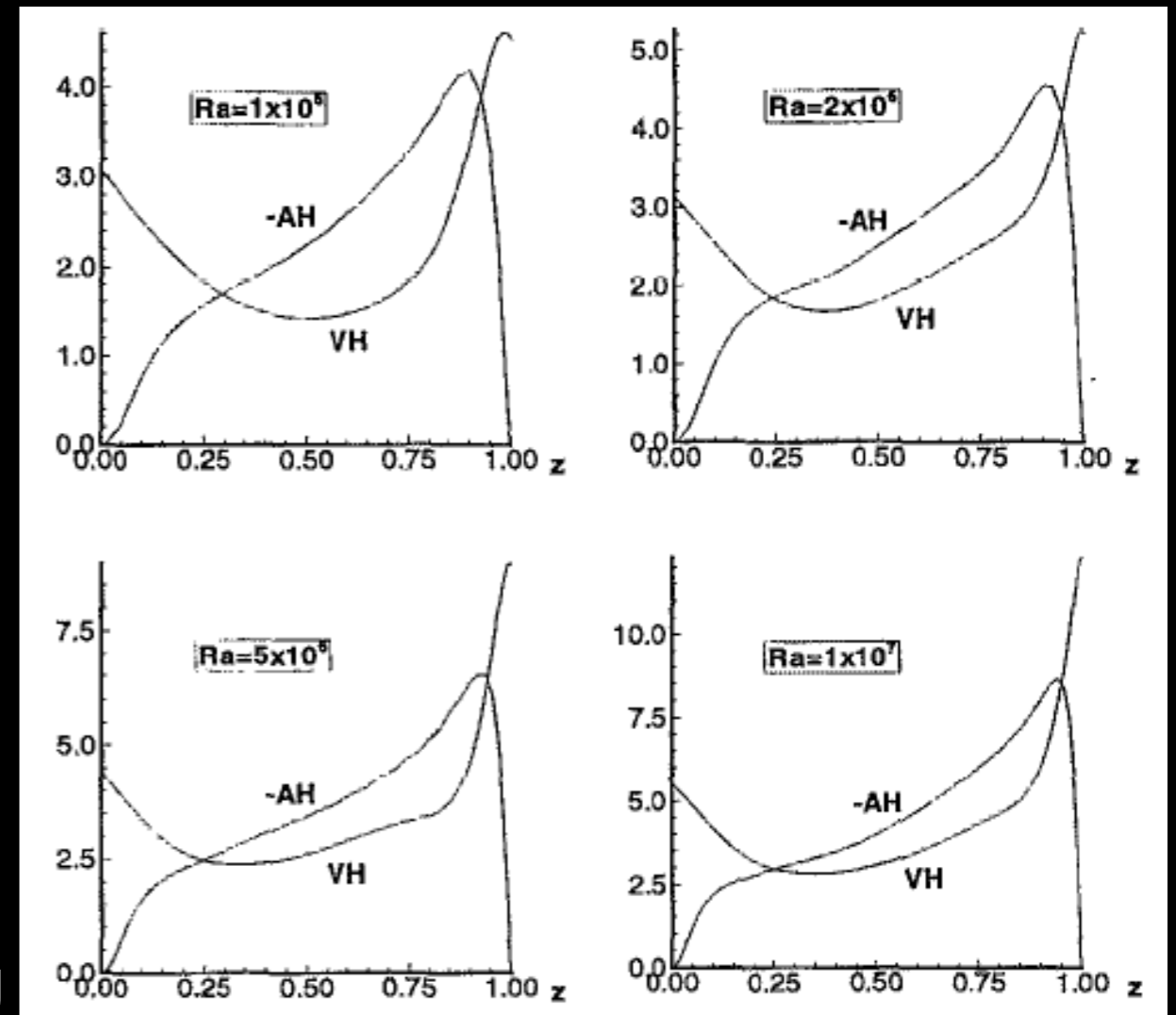
- Viscous Heating
  - always a source of heat
  - largest heating rates at boundaries



*Balachandar et al., Phys Fluid, 1993*

# Additional heating terms

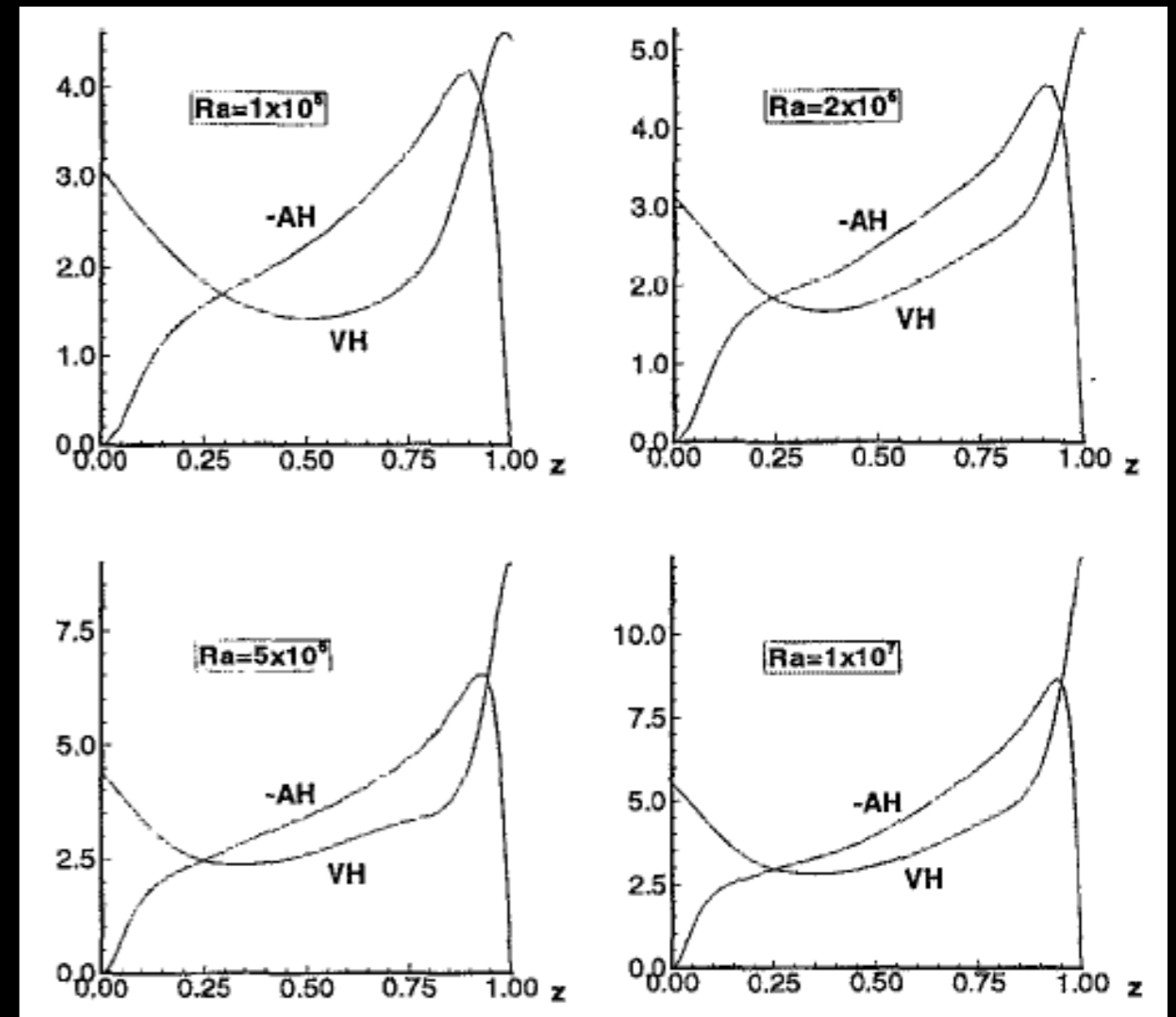
- **Adiabatic Heating**
  - effect increases with depth
  - asymmetric effect:
    - sinking slabs compress & heat, rising plumes expand & cool
    - magnitude of cooling > heating because  $T$  in plumes > slabs
  - upwellings have viscous heating and adiabatic cooling (competing)
  - downwellings have viscous heating and adiabatic heating (reinforcing)



Balachandar et al., *Phys Fluid*, 1993

# Additional heating terms

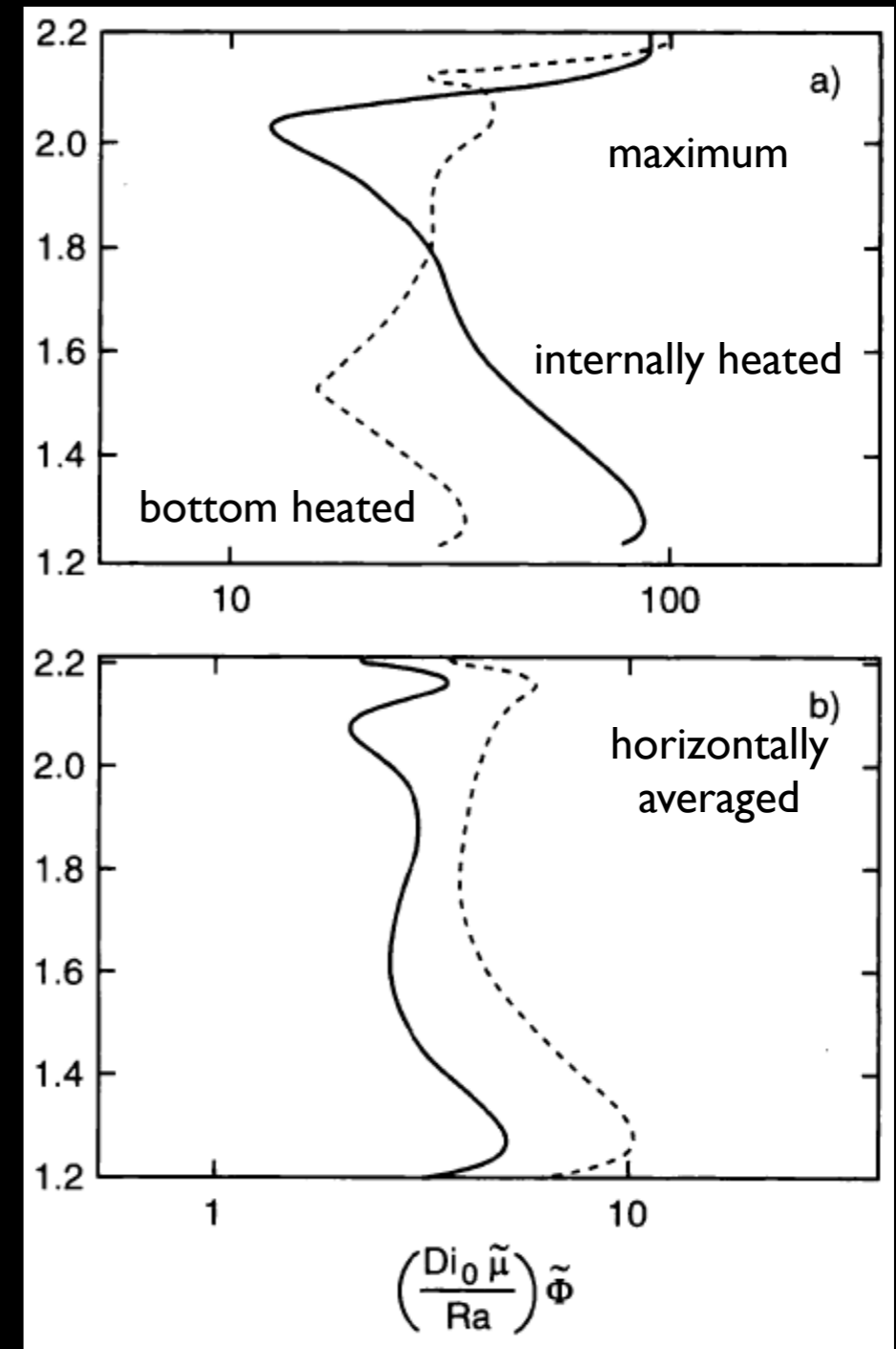
- increasingly important at higher Ra (note change in y-axis scale)
- net effect of cooling lower mantle (looks ~ an internally heated mantle)



Balachandar et al., Phys Fluid, 1993

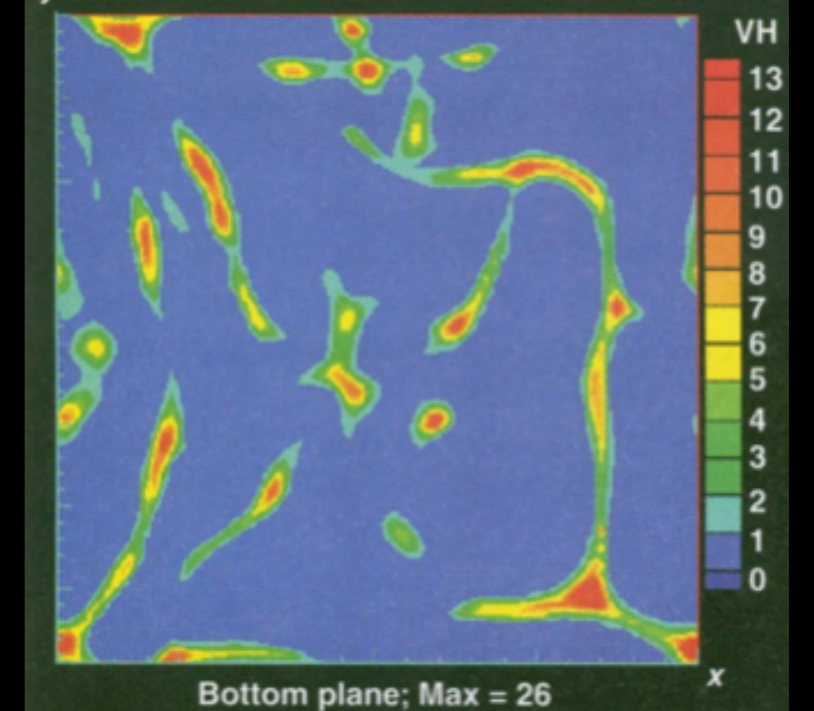
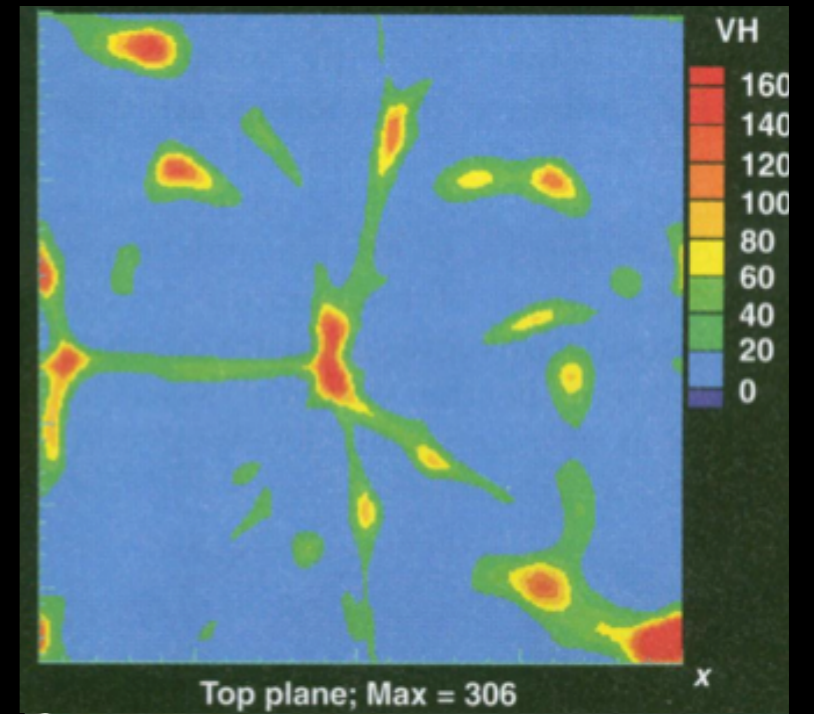
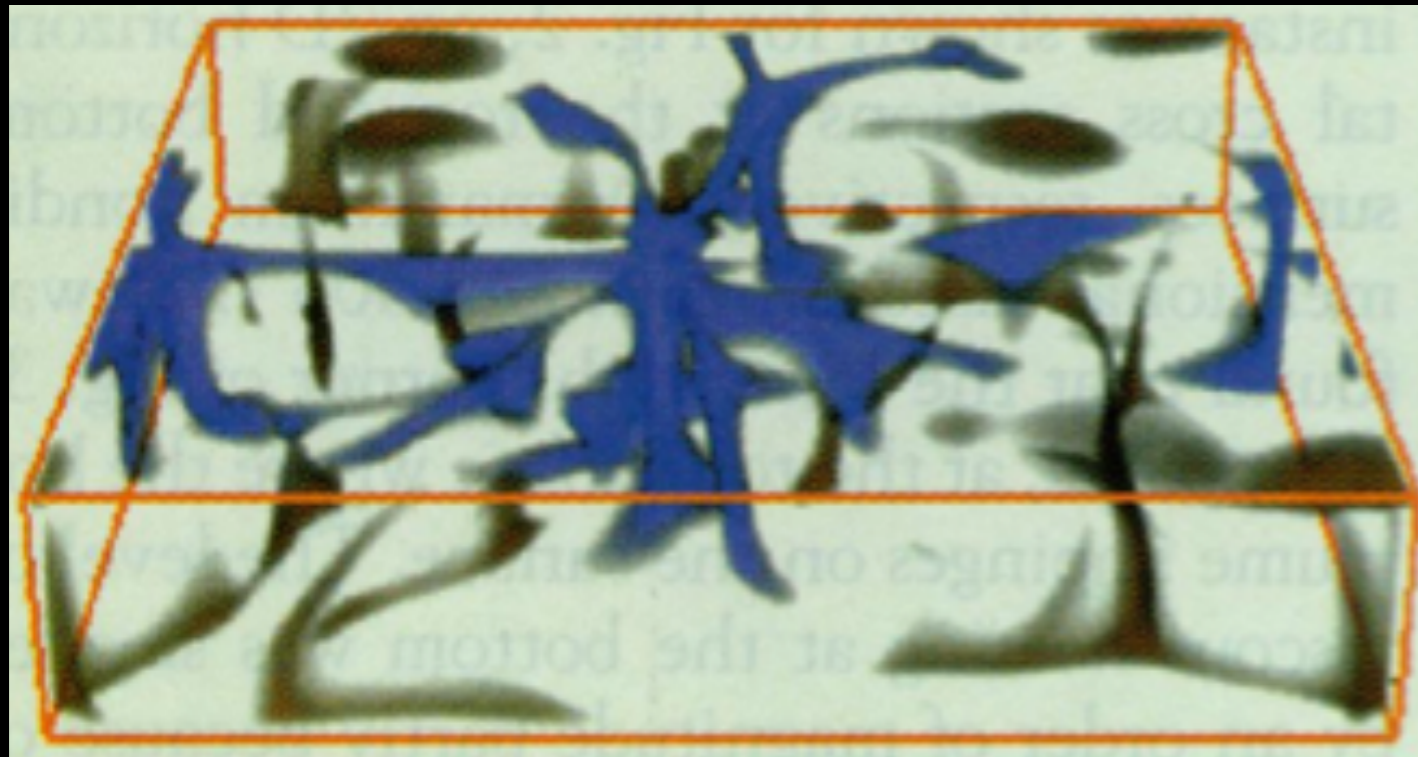
# Feedbacks between effects

- **Positive feedback between viscous/adiabatic heating and temperature-dependent viscosity**
- **Viscous heating raises temperature**
  - > **viscosity decreases**
  - > **strain-rate increases**
  - > **viscous heating increases, etc...**
- **Maximum feedback occurs in narrow downwelling regions near surface (i.e. surrounding slabs)**
- **averaged viscous heating rates are as large as radiogenic heating**
- **stronger in bottom heated models**

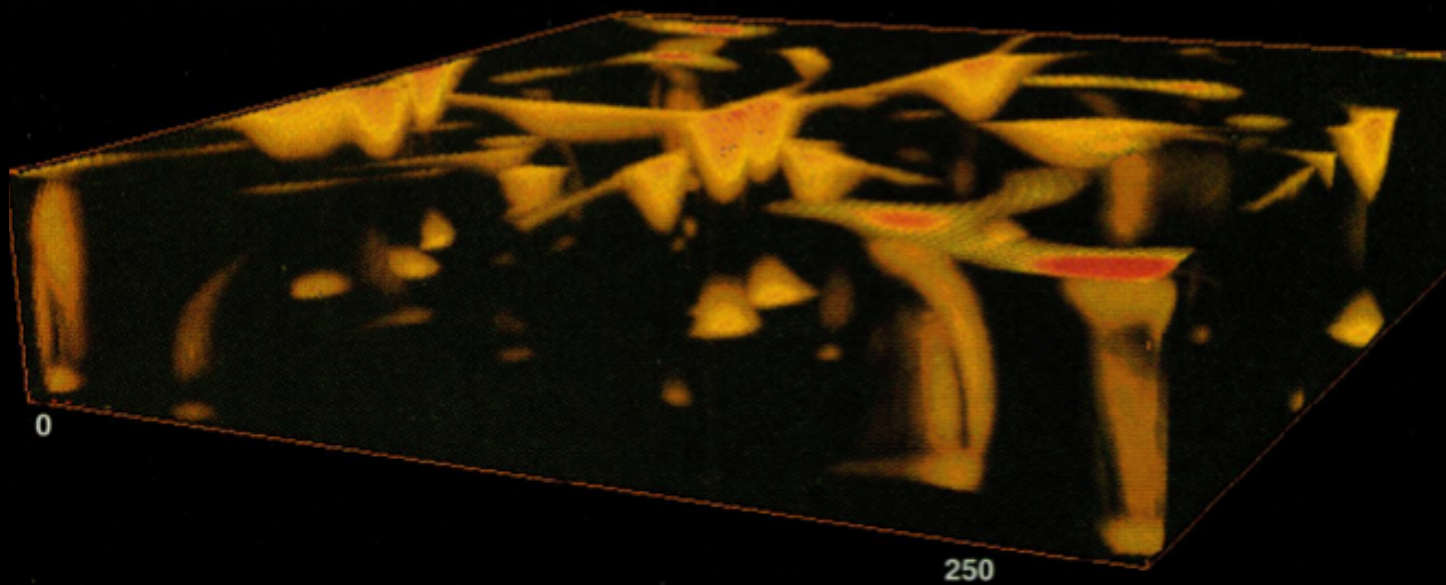


Zhang and Yuen, PEPI, 1996

# Feedbacks between effects



Balachandar et al., Science, 1995



# Bullen's parameter

- Adams-Williamson's equation

$$\frac{\partial \rho}{\partial z} = \underbrace{\frac{\rho g}{\phi}}_{\text{adiabatic density gradient}} - \underbrace{\alpha(z) \rho \left( \overbrace{\frac{\partial T}{\partial z}}^{\text{geotherm}} - \overbrace{\frac{\alpha(z) g T}{c_p}}^{\text{adiabatic temp gradient}} \right)}_{\text{non-adiabatic density gradient}}$$

# Bullen's parameter

- Adams-Williamson's equation

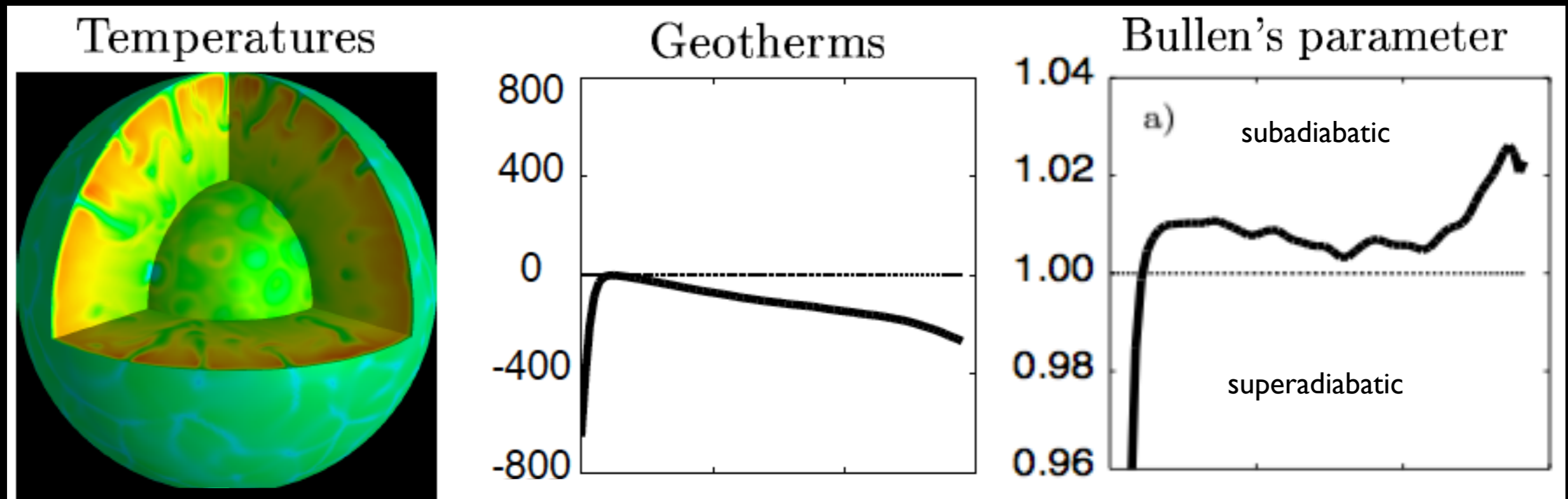
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- Bullen's parameter (measure of non-adiabaticity)

$$\Psi = 1 - \frac{\alpha(z) \phi}{g} \left( \frac{\partial T}{\partial z} - \frac{\alpha(z) g T}{c_p} \right) = \frac{\phi}{\rho g} \frac{\partial \rho}{\partial z}$$

# Is the lower mantle adiabatic?

- isoviscous, compressible, internally heated mantle at  $Ra = 1.1 \times 10^8$ ,
- lower mantle subadiabatic

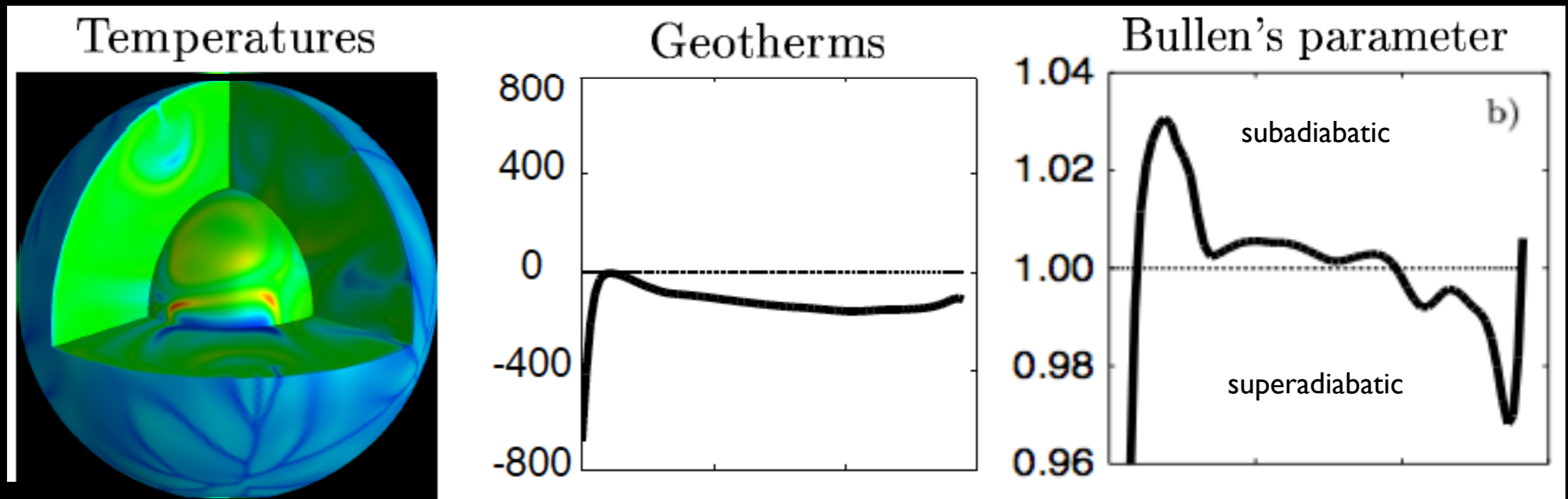


*Bunge et al, GRL, 2001*



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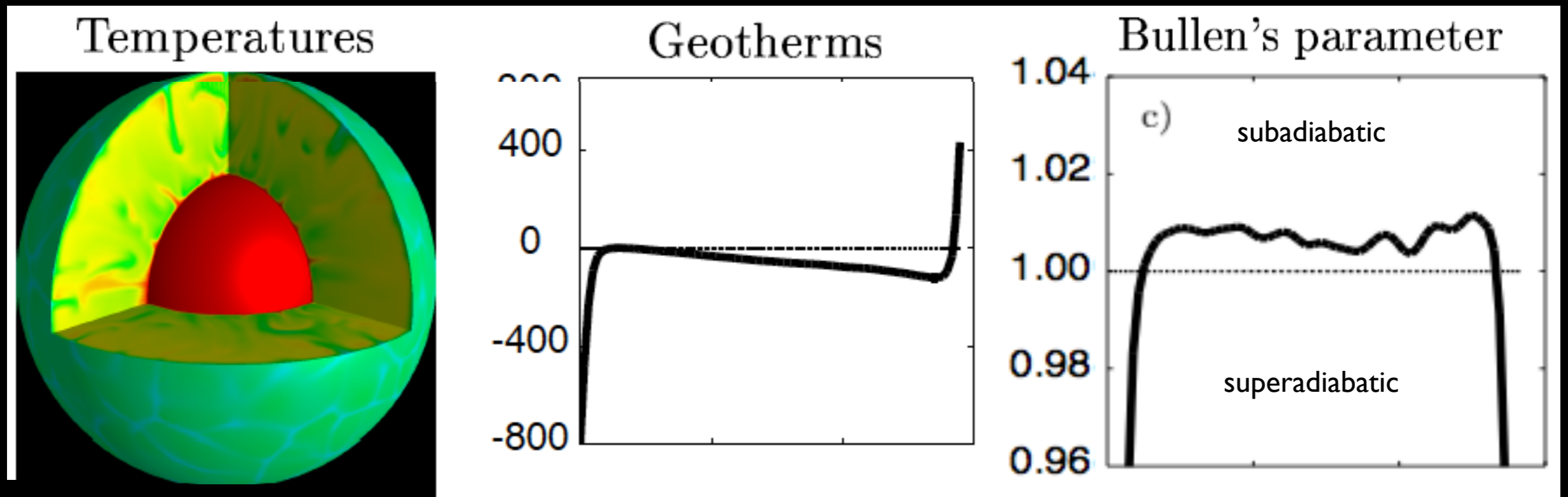
- isoviscous, compressible, internally heated mantle at  $Ra = 1.1 \times 10^8$ , lower mantle 40x more viscous
- lower mantle superadiabatic



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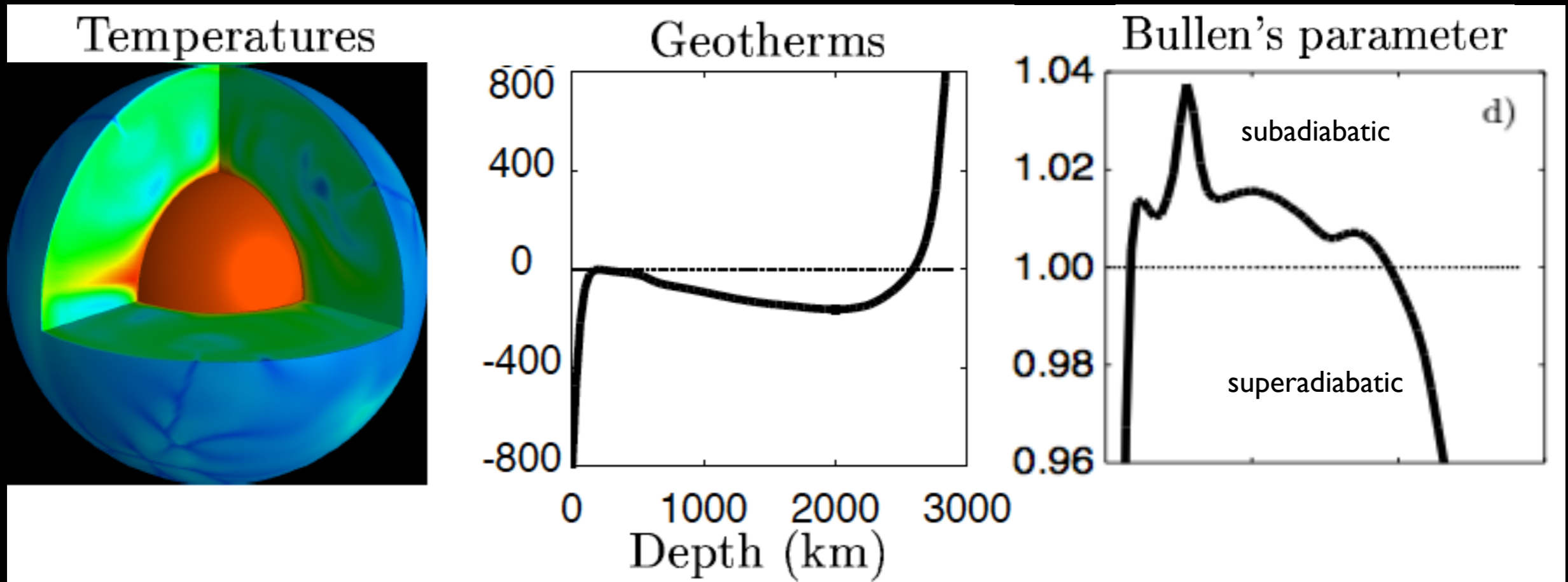
- isoviscous, compressible, bottom heated mantle at  $Ra = 1.1 \times 10^8$
- only boundary layer is superadiabatic



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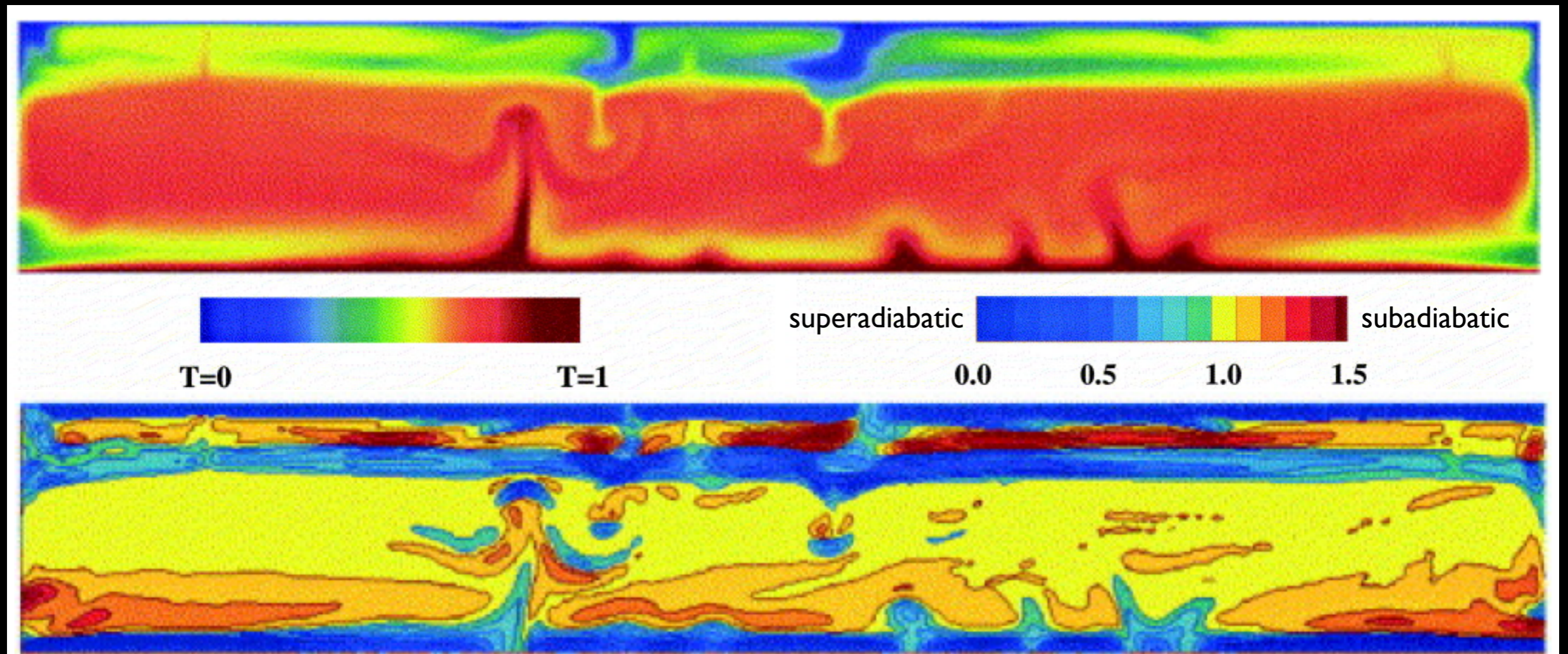
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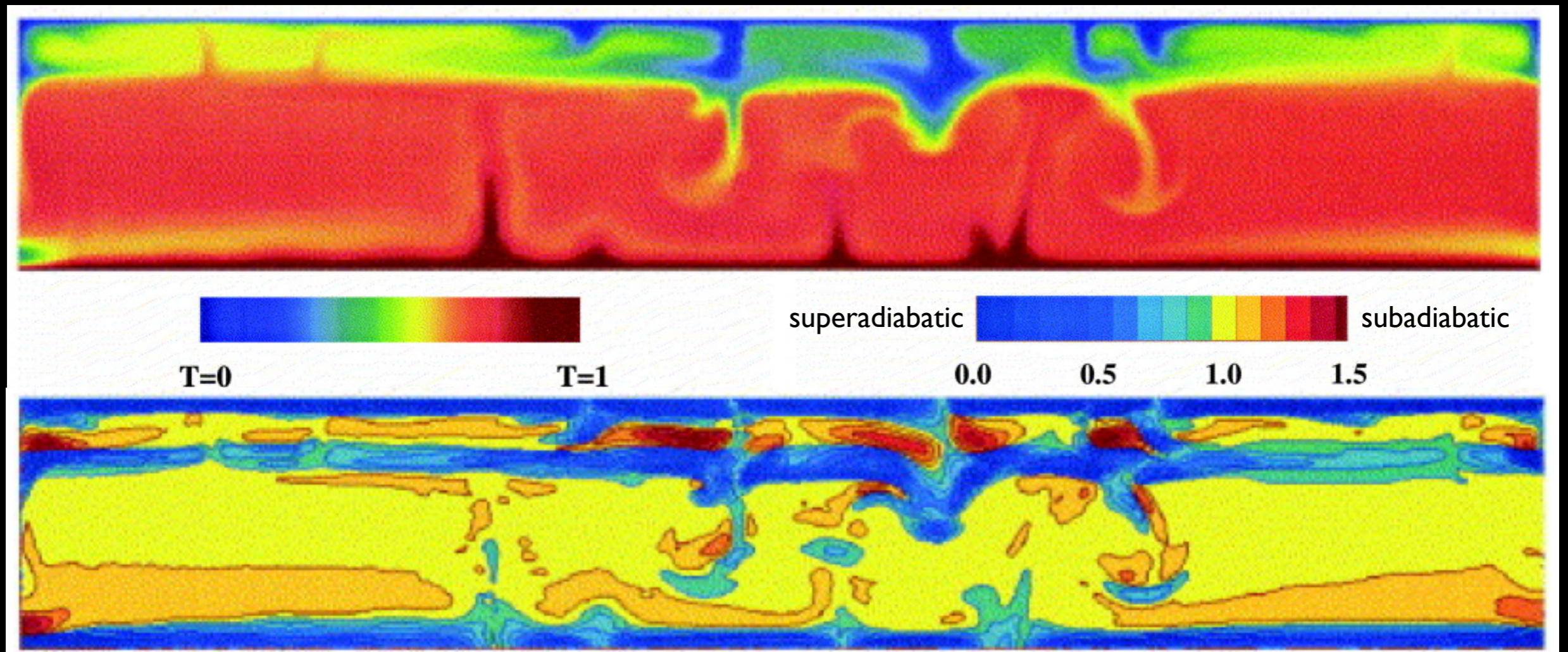
- Temperature and corresponding Bullen's parameter from compressible mantle convection



*Matyska and Yuen, EPSL, 2002*

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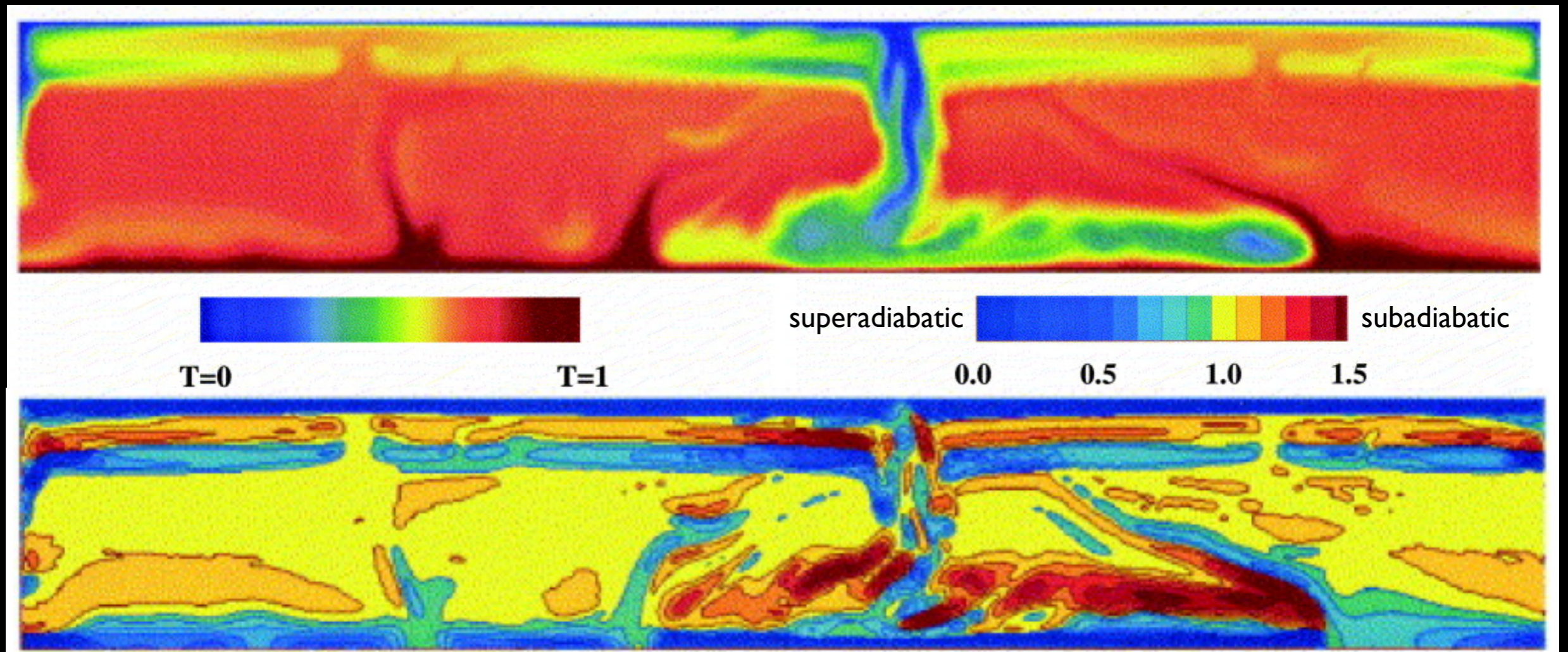
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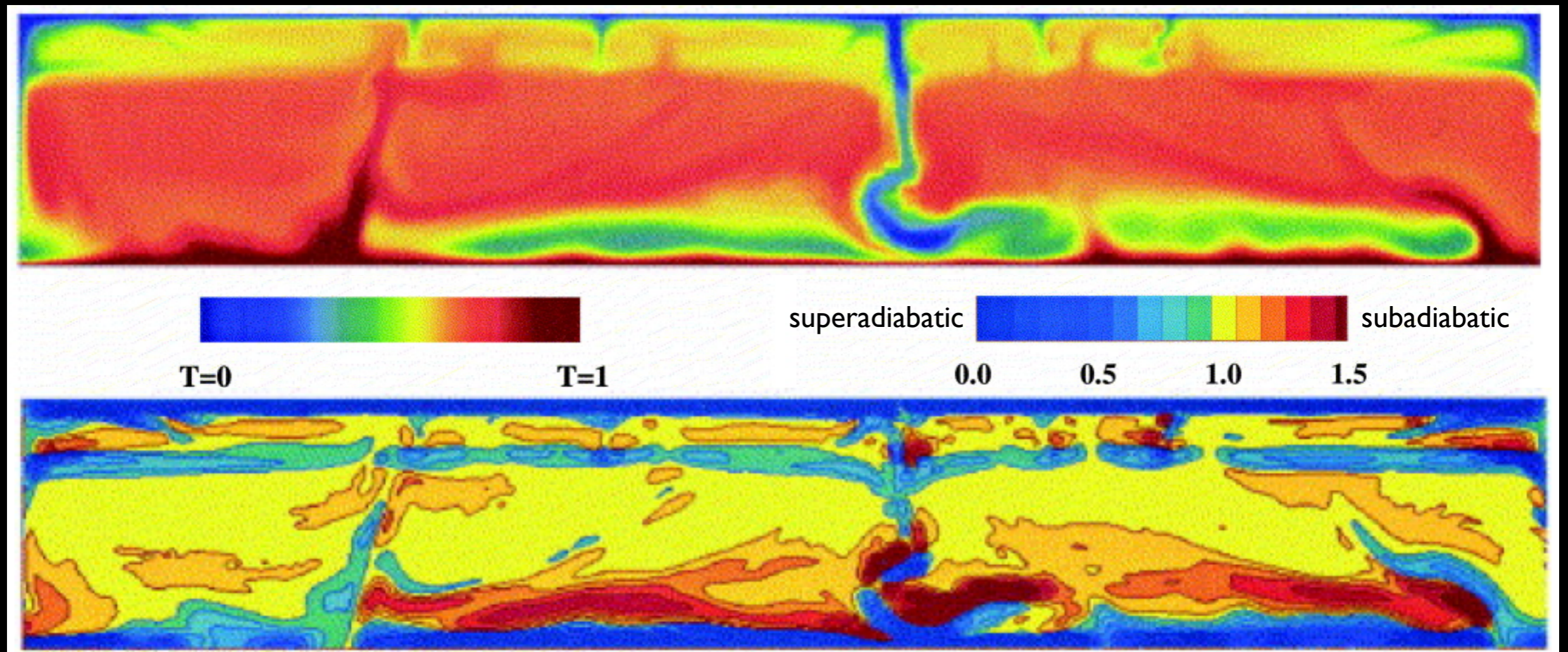
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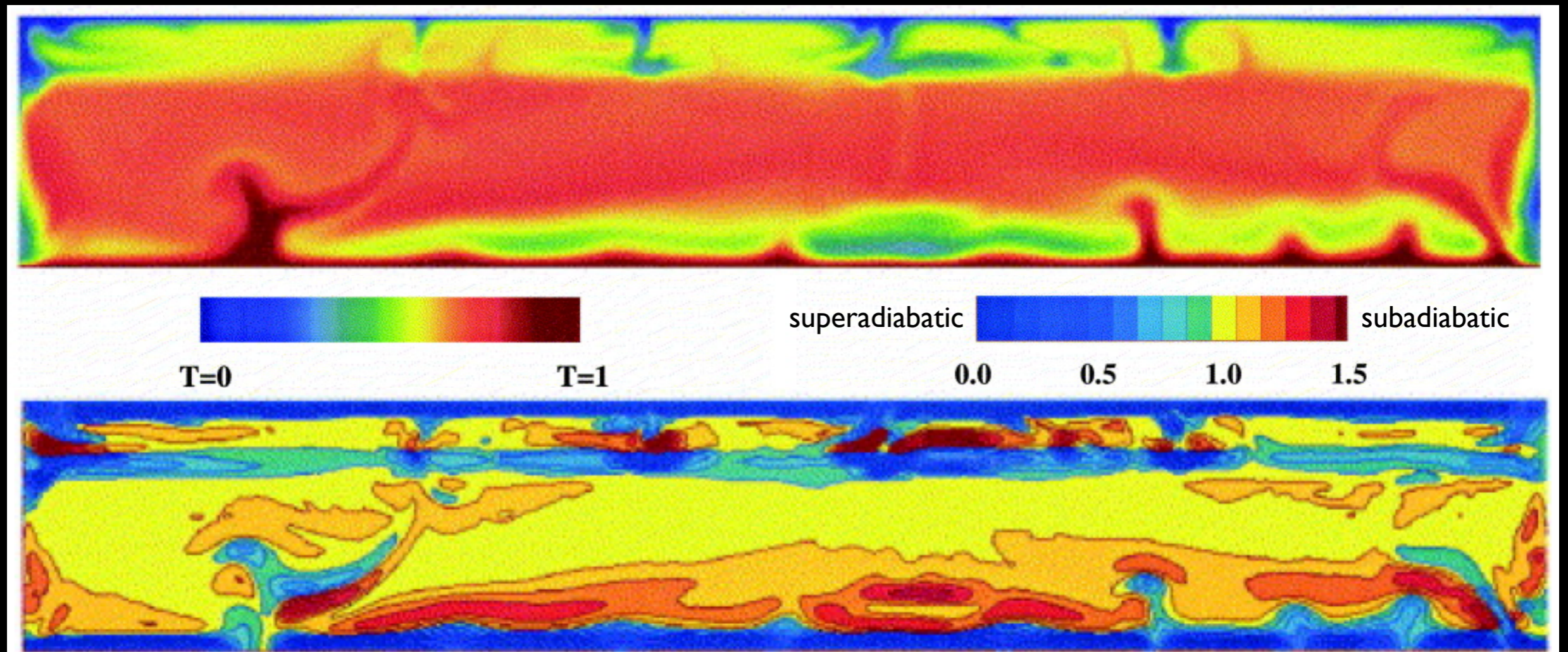
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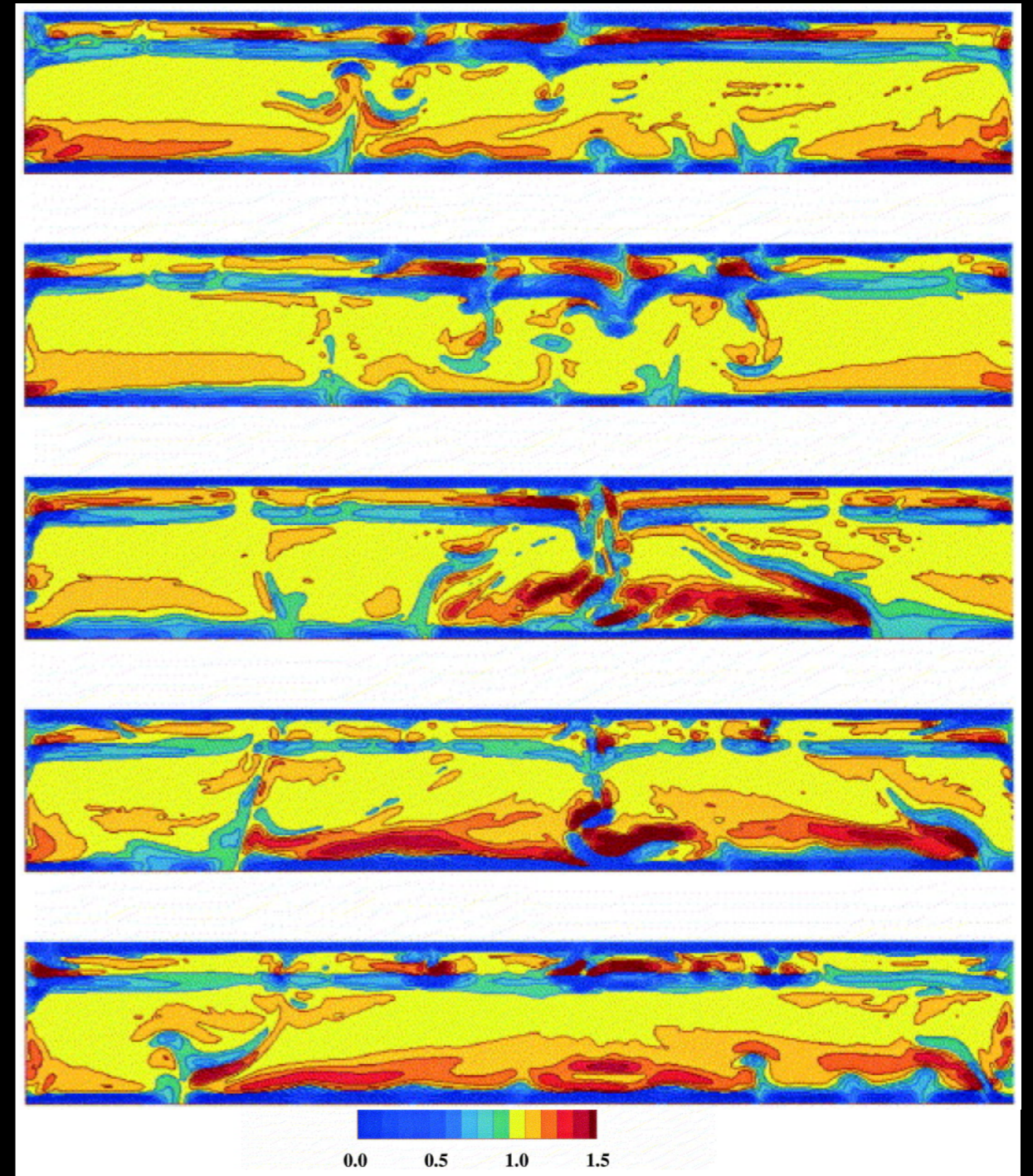
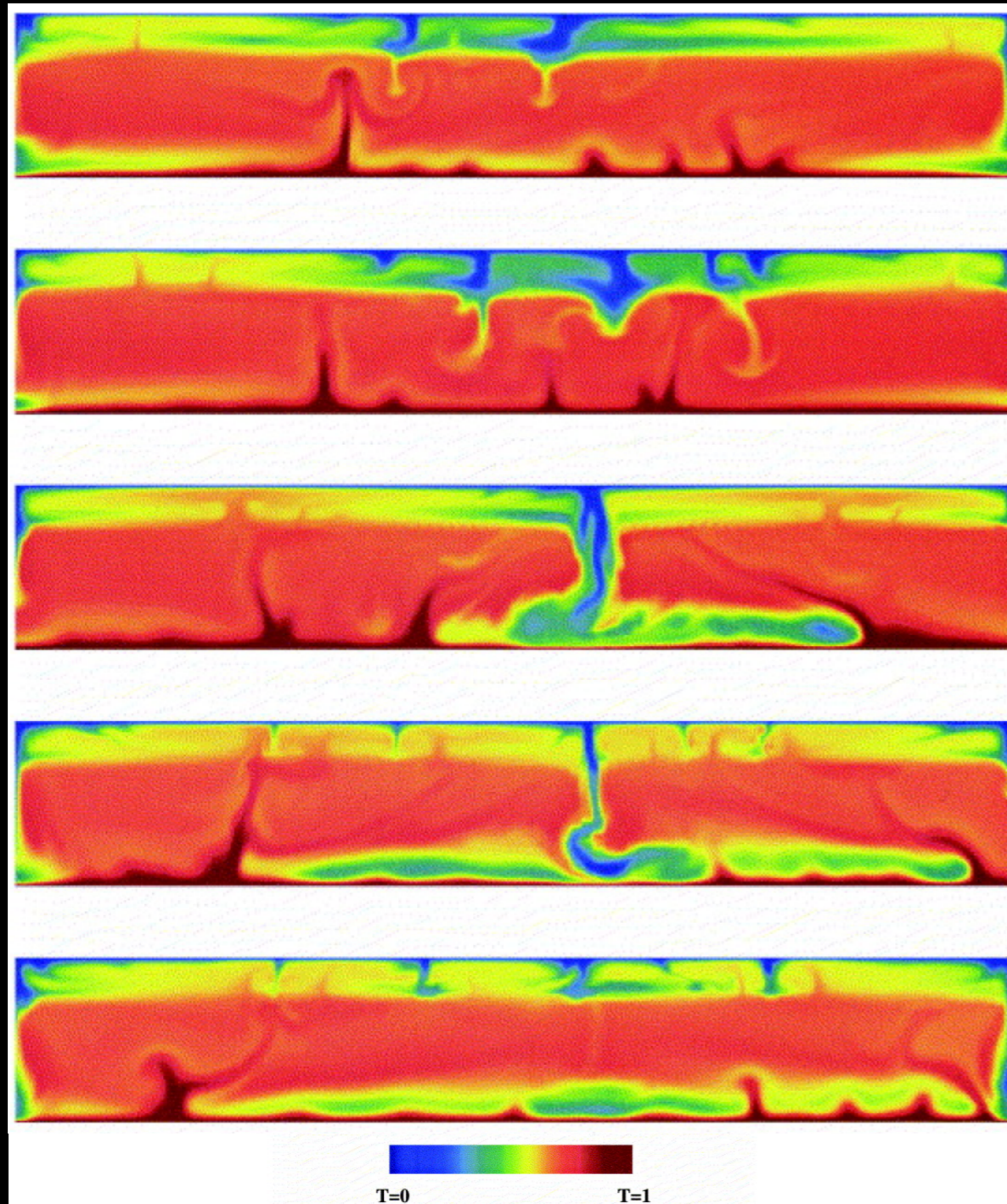
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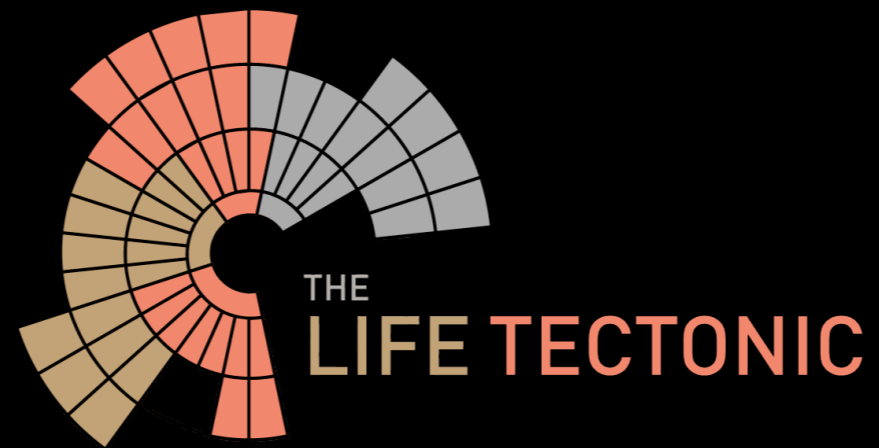
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*Matyska and Yuen, EPSL, 2002*



[www.thelifetectonic.com](http://www.thelifetectonic.com)



*Thank you! Questions??*